

# CIEM1110-1: FEM, lecture 4.1

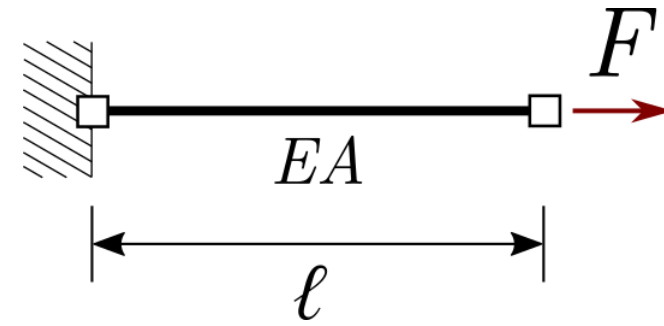
Workshop: Nonlinear material models

Iuri Rocha

## Notebook 1

Run the model as is:

- Load or displacement control?
- Convergence behavior?



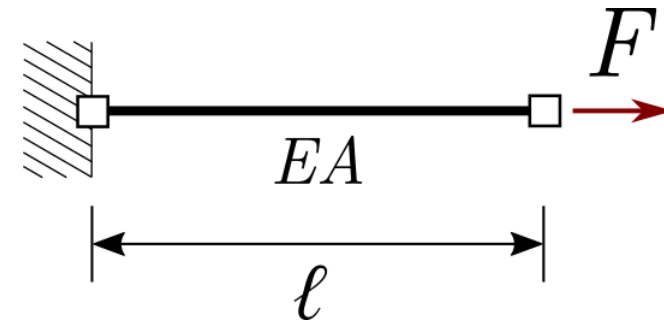
## Notebook 1

Run the model as is:

- Load or displacement control?
- Convergence behavior?

Non-consistent tangent stiffness matrix:

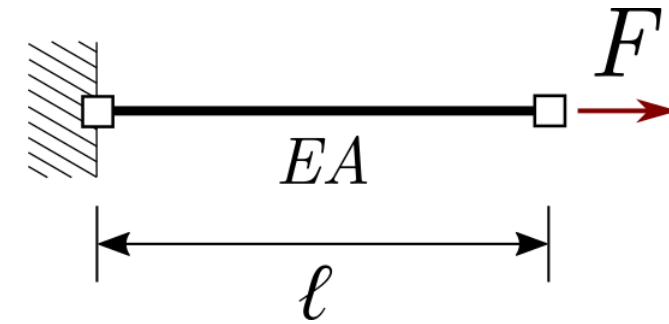
- Perturb the consistent tangent with `alpha*np.linalg.norm(strain)`
- Convergence behavior for different values of  $\alpha$ ?
- Time step size influence?



## Notebook 1

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- Load or displacement control?
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Non-consistent tangent stiffness matrix:

- Perturb the consistent tangent with `alpha*np.linalg.norm(strain)`
- Convergence behavior for different values of  $\alpha$ ?
- Time step size influence?

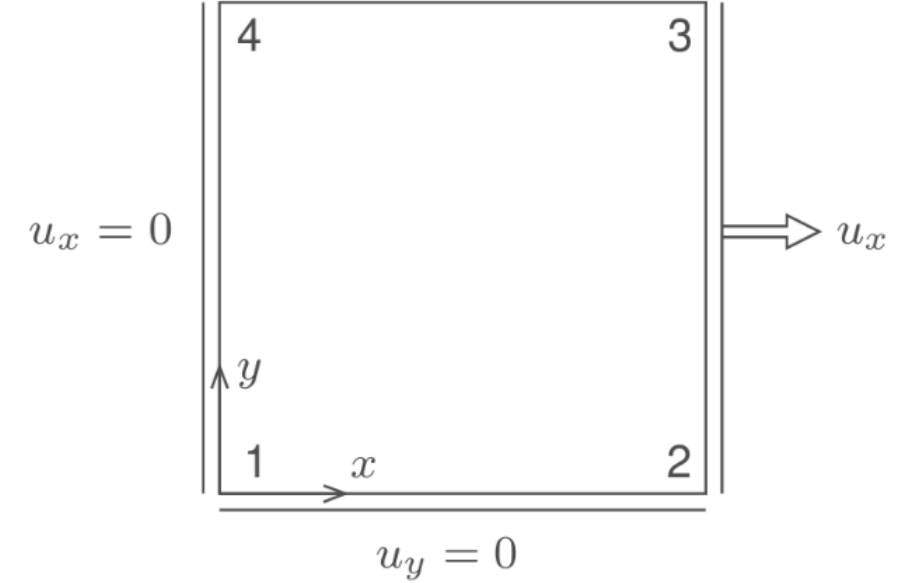
Secant stiffness:

- Change `stiff` to a constant 1000
- Convergence behavior?

## Notebook 2

Run the model as is:

- Convergence behavior?



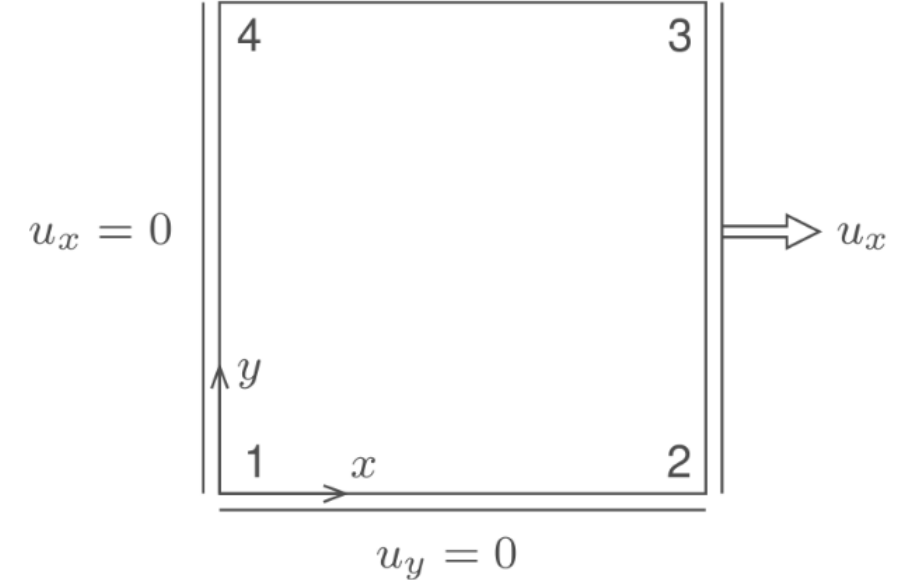
## Notebook 2

Run the model as is:

- Convergence behavior?

Try with exponential hardening:

- Change yield function to  $\sigma_y = 64.8 - 33.6 \exp\left(-\frac{\kappa}{0.003407}\right)$
- What happens to convergence?
- Does a smaller time step help?



## Notebook 2

Run the model as is:

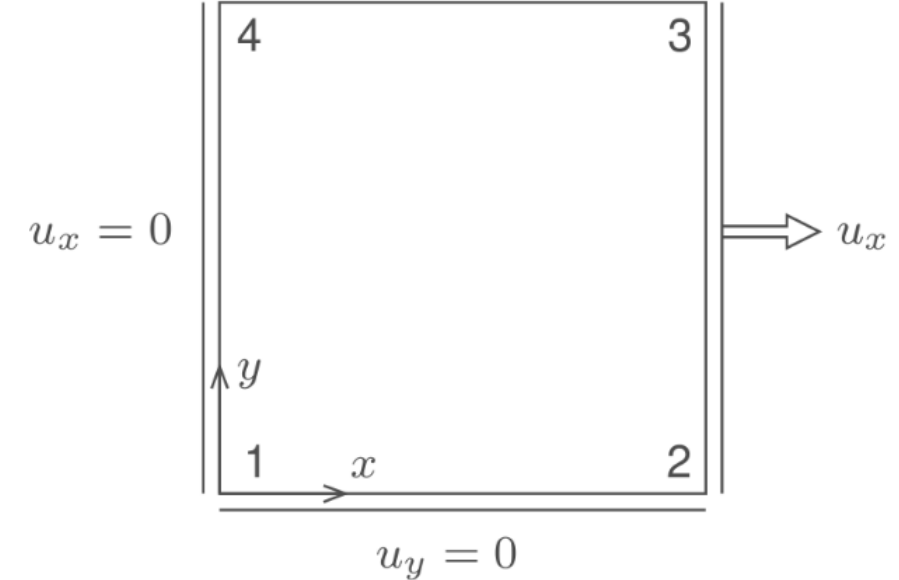
- Convergence behavior?

Try with exponential hardening:

- Change yield function to  $\sigma_y = 64.8 - 33.6 \exp\left(-\frac{\kappa}{0.003407}\right)$
- What happens to convergence?
- Does a smaller time step help?

Switch to displacement control:

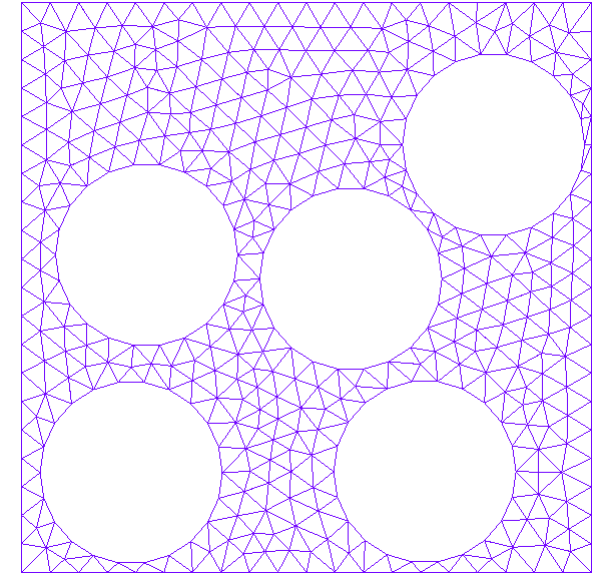
- Convergence behavior?
- Try with Modified Newton-Raphson



## Notebook 3

Run the model as is:

- How are the BCs evolving in time?
- How is  $\kappa$  evolving?
- How is strain distribution changing with time?





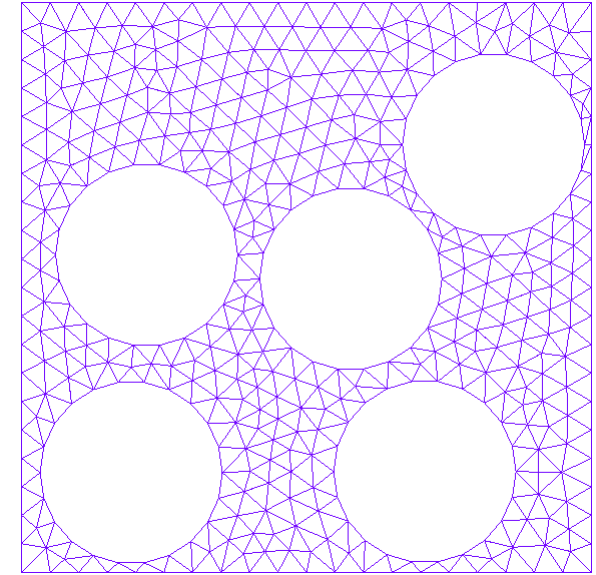
## Notebook 3

Run the model as is:

- How are the BCs evolving in time?
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- How is strain distribution changing with time?

Non-monotonic displacement path:

- Change the `timeSignal` and run the model
- How is the average plastic strain changing in time?
- Look at the evolution of  $\kappa$ , what is happening?



## Notebook 3

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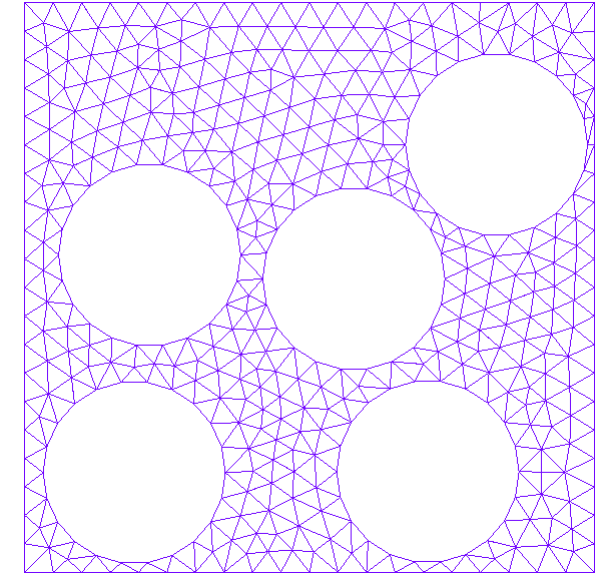
- How are the BCs evolving in time?
- How is  $\kappa$  evolving?
- How is strain distribution changing with time?

Non-monotonic displacement path:

- Change the `timeSignal` and run the model
- How is the average plastic strain changing in time?
- Look at the evolution of  $\kappa$ , what is happening?

Try a more complex path:

- How are  $\kappa$  and the strains changing in time?



# Outlook

This week:

- Viscoelasticity with Cor Kasbergen
- Workshop on Thursday – first graded assignment

Next week:

- Lattice methods with Branko Šavija