

TECHNOLOGICAL UNIVERSITY DELFT

DEPARTMENT OF AERONAUTICAL ENGINEERING

Report VTH-124

THEORETICAL AND EXPERIMENTAL INVESTIGATIONS
OF INCOMPRESSIBLE LAMINAR BOUNDARY LAYERS
WITH AND WITHOUT SUCTION

Ph.D THESIS

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DELFT
the NETHERLANDS

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This PDF-file contains chapter 13:

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